Data Security Analysis Against Chosen Ciphertext Secure Public Key Attack Using Threshold Encryption Scheme

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ABSTRACT
A public key encryption cryptography system can be utilized to generate ciphertext of a message using a public key. However, this public key encryption cryptography system cannot be utilized if you want to generate ciphertext using several different keys. Solving the problems above can use the Chosen Ciphertext Secure Public Key Threshold Encryption scheme but are the securities from Threshold Encryption really strong in securing messages, therefore the above problems can be analyzed for Data Security Against Chosen Ciphertext Secure Public Key Attacks Using Threshold Encryption Schemes. The work process starts from Setup which functions to generate the server's private key and public key. Then, the process is continued with ShareKeyGen which functions to generate private keys based on the user's identity. After that, the process continues with ShareVerify which serves to verify the key generated from the ShareKeyGen process. The process will be continued again with Combine which serves to generate a private key that will be used in the decryption process. After that, the process will continue with the encryption process of the secret message. The ciphertext obtained will be sent to the recipient. The receiver verifies the ciphertext by running ValidateCT. Finally, the ciphertext is decrypted by running Decrypt. The software created can be used to display the workflow process of the Threshold schema. In addition, it makes it easier to test intercepts of ciphertext messages to other users so that generic securities analysis is carried out in testing the resulting ciphertext. The results of the implementation of Threshold Encryption algorithm scheme can protect important personal data, because it involves human rights, namely the right to access, the right to delete, the right to correct, the right to be corrected and the right to transfer personal data safely from attacks.

KEYWORDS
Chosen Ciphertext Secure Public Key Threshold Encryption Without Random Oracle; ciphertext; encryption; decryption

INTRODUCTION
In a threshold public key encryption system, the private key is conveyed among n decoding servers so that at slightest k servers are required for the decoding prepare. In a edge encryption framework, an substance called a combiner incorporates a C ciphertext that it needs to unscramble. The combiner sends C to the unscrambling server and gets the unscrambling parcel from at slightest k of n decoding servers, where k ≤ n. Then, the combiner will combine these k decryption parts in a complete decryption of C. Ideally, no other interaction is required on the system, as the servers do not need to communicate with
each other during the decryption process. This threshold system is called non-interactive. Sometimes, it is necessary for the decryption threshold to be robust, where if the decryption threshold of a substantial ciphertext comes up short, the combiner can recognize the decoding server that provided the invalid decryption part.

This construction consists of two stages. First, the CCA construction from Canetti and partners was developed into a threshold system. Second, a robust threshold version of the Identity Based Encryption (IBE) scheme is provided by Boneh and Boyen. The robustness of this scheme is obtained by including a number of inner checks to the system. In cryptography, an irregular prophet is an prophet (hypothetical dark box) that reacts to each inquiry with a reaction that's chosen arbitrarily and consistently from its output domain. Or in other words, a irregular oracle may be a scientific work that maps a conceivable inquiry with a irregular reaction from its output domain.

Based on the depiction of the foundation above, the problems encountered can be formulated as follows:

1. The ordinary public key encryption scheme cannot use multiple keys to generate the ciphertext of a message for distribution and the threshold encryption scheme, makes the combiner unable to identify the decryption server used to decrypt the message.
2. Proof of generic security by implementing a threshold encryption scheme against attacks from Chosen Ciphertext Secure (CCA).

The purpose of this study is to apply a public key encryption threshold scheme to produce ciphertext that can be returned using several keys and can verify the ciphertext that will be used to decrypt the message. The combiner then performs a generic security proof analysis of the threshold encryption algorithm whether it is really safe and strong against attacks from Chosen Ciphertext Secure (CCA). Thus, data security in the network system can be avoided from threats such as access, theft, changes to data destruction caused by viruses, sniffing or attacks (Nasution, A.M., et al. 2021).

LITERATURE REVIEW

Threshold Public Key Encryption
A threshold public key encryption system may be a open key framework in which the private key is disseminated among n decoding servers such that a least of k servers is required for the decoding handle. The combiner sends C to the unscrambling server and gets the decoding parcel from at slightest k of n decoding servers, where k ≤ n. Then, the combiner will combine these k pieces of unscreaming into a total decoding of C.

Threshold Identity Based Encryption System
In 2005, Dan Boneh, Xavier Boyen and Shai Halevi introduced a threshold encryption system that is secure against chosen ciphertext attacks (CCA) without arbitrary oracle. The following describes a concrete Threshold IBE (TIBE) system. The operating principle of the TIBE system is as follows:

1. Setup(n, k, A): By running GG(λ) to generate a bilinear group G of order prime p > n. Choose a random generator g, g2, h1 on G, and a random polynomial of degree k – 1, f ∈ Zp[X]. Set α = f(0) Zp and g1 = gα.

The PK system parameters comprise of PK = (G, g, g1, g2, h1). For i = 1, ..., n, the master key share (i, SKi) of server i can be characterized as SKi = giαi. The VK public verification key consists of n-tuples (g i f(1), ..., g i f(n)).
2. **ShareKeyGen**\( (PK, i, SK_i, ID) \). Let \( PK = (G, g, g_1, g_2, h_1) \) and take a arbitrary number \( r \in \mathbb{Z}_p \). This algorithm generates the private key \( \theta_i = (i, (w_{i,0}, w_{i,1})) \) using the following formula:

\[
    w_{i,0} = SK_i \cdot (g_1^{ID} h_1)^r \quad \quad w_{i,1} = g^r
\]

\[\text{Equation (1)}\]

3. **ShareVerify**\( (PK, VK, ID, \theta_i) \). To confirm that \( \theta_i \) is a valid private key subset for identity \( ID \), assume \( VK = (u_1, \ldots, u_n) \) where \( u_i = g^{f(i)} \) and \( \theta_i = (i, (w_{i,0}, w_{i,1})) \). This algorithm returns valid or invalid based on the taking after conditions:

\[
    e(u_i, g_2) \cdot e(g_1^{ID} h_1, w_{i,1}) = e(g, w_{i,0})
\]

\[\text{Equation (2)}\]

4. **Combine**\( (PK, VK, ID, \theta_1, \ldots, \theta_k) \). If any of \( \theta_1, \ldots, \theta_k \) is invalid, or if two parts \( \theta_i \) and \( \theta_j \) produce the same server index \( i \), then return to \( \perp \) and exit. If not, then assume \( \theta_i = (i, (w_{i,0}, w_{i,1})) \). Accept that decryption server \( i = 1, \ldots, k \) is used to generate \( \theta_1, \ldots, \theta_k \). To determine the private key for \( ID \), suppose \( \lambda_1, \ldots, \lambda_k \in \mathbb{Z}_p \) is the Lagrange coefficient so that \( \alpha = f(0) = \sum_{i=1}^{k} \lambda_i f(i) \). This algorithm generates the private key \( d_ID = (w_0, w_1) \) using the following equation:

\[
    w_0 = \prod_{i=1}^{k} w_{i,0}^{\lambda_i} \quad , \quad w_1 = \prod_{i=1}^{k} w_{i,1}^{\lambda_i}
\]

\[\text{Equation (3)}\]

5. **Encrypt**\( (PK, ID, M) \): Encrypt \( M \in G_1 \) as ID identity, select a arbitrary number \( s \in \mathbb{Z}_p \) and generate:

\[
    C = \left( e(g_1, g_2)^s \cdot M, \quad g^s, \quad g_1^{ID} h_1^s \right)
\]

\[\text{Equation (4)}\]

6. **ValidateCT**\( (PK, ID, C) \). To approve a ciphertext \( C = (A, B, C_1) \) for an ID identity, this algorithm returns substantial or invalid depending on the following equation:

\[
    e(B, g_1^{ID} h_1) = e(C_1, g)
\]

\[\text{Equation (5)}\]

7. **Decrypt**\( (PK, ID, d_ID, C) \). To decrypt \( C = (A, B, C_1) \) using a private key \( d_ID = (w_0, w_1) \), to begin with check ValidateCT \( (PK, ID, C) = valid \) \( e(g_1, g_2) \cdot e(g_1^{ID} h_1, w_1) = e(g, w_0) \). If any of the checks fail, output \( \perp \) and exit. Otherwise, generate plaintext using the following formula:

\[
    A \cdot e(C_1, w_1) / e(B, w_0)
\]

\[\text{Equation (6)}\]
RESEARCH METHODS

The working procedure of a secure threshold encryption system against a chosen ciphertext attack (CCA) can be detailed as shown in the following activity diagram:

**Figure 1. Activity Diagram of the System**
System Modeling

The tool used to analyze and model the system is a use case. The following figure shows the use case of the system:

![Use Case Diagram of the System](image)

**Figure 2. Use Case Diagram of the System**

RESULTS AND DISCUSSION

The results of the analysis of attacks from chosen ciphertext attacks (CCA) can be categorized as follows:

1. Complex calculation process and uses several other algorithms to help generic securities from Threshold Encryption

![Generic display of numbers in setup](image)

**Figure 3. Generic display of numbers in setup**
**Wiretapping Test**

1. **Different Server Options**

   The encryption process is carried out on the input message 'Khairunas, USU’s master student of informatics engineering', if the message interceptor made an error in selecting the server, even though it succeeded in validating the encryption threshold scheme, it will not be able to find out that the message did not come from the real sender, it can be proven by the display following:

   ![Encryption Process Display](image)

   **Figure 6.** Encryption Process Display

If the selected *server* does not follow the encryption process, then the decryption process will fail, and here there will be provisions of the encryption threshold algorithm for the minimum server used in every message delivery given to the recipient as shown in the following figure:
2. Ciphertext Replacement
If the ciphertext is replaced, the text to be decrypted will experience an oddity in the form of the decrypted words will become an incomprehensible language so that it can be seen that the message does not come from the actual sender and can be proven by the following picture:

Figure 7. Process Display, Wrong Server Choice

Figure 8. Display of the Ciphertext Replacement Process
Discussion

Based on the results of experiments carried out on testing the Threshold Encryption algorithm using the SHA-1 hash function that and at least using 2 servers as part of the decryption, the resulting m value is 320 bits even though the message lengths are different, thus increasing the security generated against the strength of the message security alert. In the verification and validation of the created message, the values generated using the weil pairing function e are values to produce in the form of signatures or points such as coordinates of curve points which are linear and the level of security is relatively complicated because it uses an elliptic curve discrete logarithm problem other than It is also a prime number which is relatively prime helping the level of security that produces only 1 inverse number for each message sent with different key formations.

Based on the testing process, it can be obtained from the analysis results, namely the encryption and decryption time of the message m into a value in binary form using the hash function SHA-1 does not experience a time difference with the same amount but is more effective because the results issued by SHA-1 are greater, namely 320 bits. that the algorithm that has been tested produces a better level of security because it produces output to 320 bits from the previous scheme. And from the calculation results, the complexity of the inverse value is more to return the point value based on the elliptic bend discrete logarithm issue because the values are taken randomly. This value makes it more complex and produces a safer level of security even though with the same character but the difference in the output of the point value generated from different signatures.

CONCLUSION

After completing this research, the author draws several conclusions:

1. The process flow section of the Threshold Encryption Scheme can be used to help understand how it works for users who have studied and understood the basic concepts of cryptography.
2. The algorithm scheme of Threshold Encryption can be used to secure text-based document file data, to protect important personal data, because it involves human rights, namely the right to access, delete, corrected and transfer personal data securely from attacks.
3. From the results of the tests carried out, information is obtained that in the analysis of Data Security Against Selected Ciphertext Secure Public Key Attacks Using Threshold Encryption Scheme, if there is a ciphertext replacement, the original secret message data cannot be recovered.

REFERENCES


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